

## Summer Assignment

### Precalculus

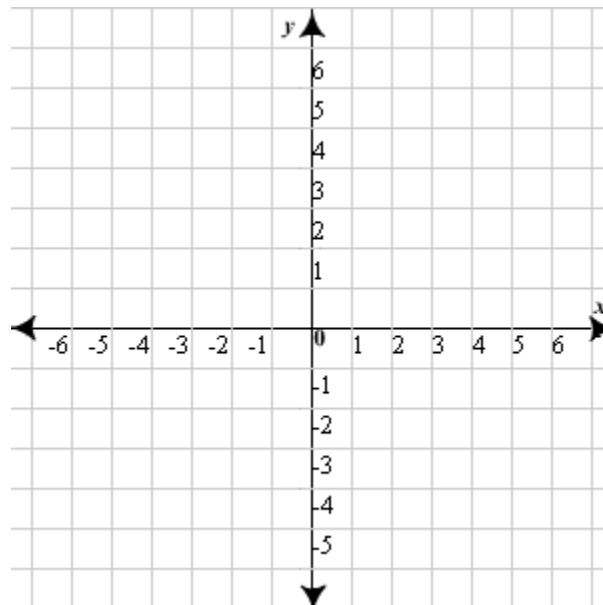
Name: \_\_\_\_\_

*Be sure to show all work and box all final answers when appropriate.*

1) Find the equation of the line that goes through the points  $(-6, -1)$  and  $(4, -3)$  in slope-intercept form.

2) Write the equation of the line that passes through the point  $(-3, 5)$  and is perpendicular to the line  $y = -2$  in any form.

3) Graph the function,  $f(x) = -|x - 3| + 1$



For #4 – 5, simplify the following complex expressions. Write all complex numbers in standard form.

4)  $(3 - 2i)(5 + i)$

5)  $\frac{5 + i}{2 - 3i}$

6) For the following quadratic equation, find the coordinates of the vertex, and the x and y intercepts. Be sure to show your work.  $y = 2x^2 - 3x - 5$

7) Given that  $f(x) = x - 5$  and  $g(x) = x^2 + 3$ , find the following:

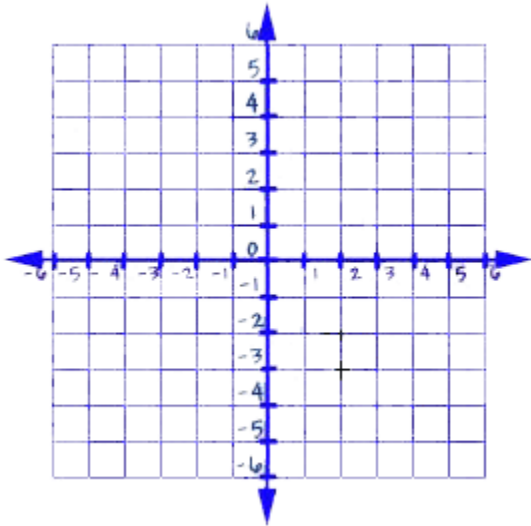
a)  $f(g(-2))$

b)  $g(f(x))$

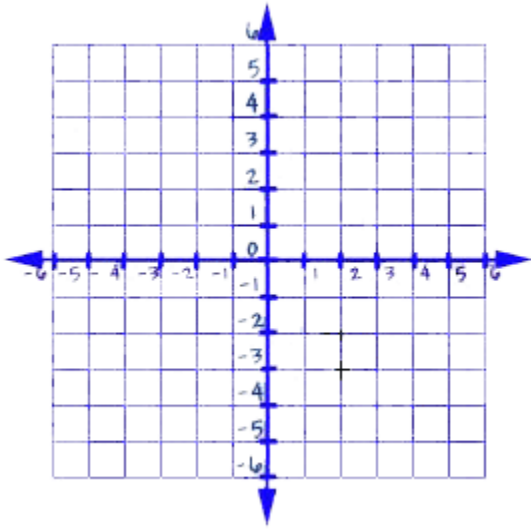
c)  $f(f(x))$

For #8 and #9, solve the following inequalities by sketching a graph on the coordinate plane provided.

8)  $y < \frac{1}{2}x - 3$



9)  $y \geq 5x^2 - 2x - 6$



10) Solve the following for  $x$ , by using the quadratic formula.  $x^2 - 5x + 9 = 0$

11) Divide  $2x^3 - 3x^2 - 5x - 12$  by  $x - 3$  using synthetic division and write a summary statement in fraction form.

For #12 – 13, list the domain for each of the following functions.

12)  $f(x) = \sqrt{x - 3}$

13)  $g(x) = \frac{x + 3}{x - 5}$

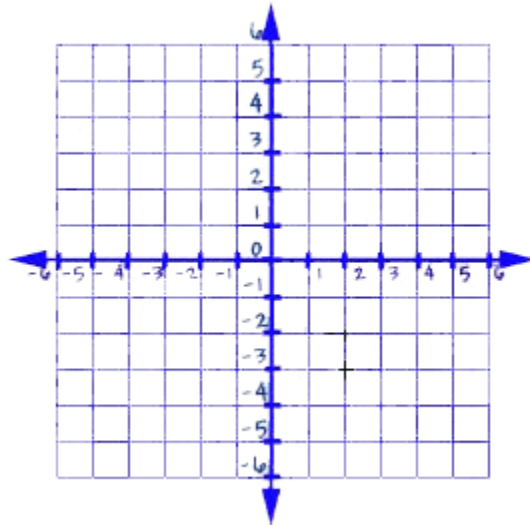
For #14 – 15, find the inverse of  $f(x)$ .

14)  $f(x) = \{(3, \frac{1}{2}), (-5, 4), (2, 1), (-4, 0)\}$

15)  $f(x) = x^2 - 3$

16) Give a sketch of the following function. What is the domain and the range? What is(are) the y-intercept(s)? What is the equation of the asymptote?

$$f(x) = (2)^{x-3} + 1$$



For #17 – 18, given the function  $f(x) = (\frac{1}{2})^{x+1} - 2$ , find the following.

17)  $f(0)$

18)  $f(-2)$

For #19 – 21, list whether each function is exponential growth or decay. Explain your answer.

19)  $f(x) = 3\left(\frac{1}{4}\right)^x - 2$

20)  $g(x) = (2)^{-x} + 1$

21)  $h(x) = 3(3)^{x+3}$

22) Expand the following logarithm:  $\log_2 \frac{x^2}{y^3 z}$

23) Condense the following logarithm:  $\ln 3 - 2\ln 5 + \frac{1}{2}\ln 9$

24) Use the change of base formula to simplify the following logarithm. Round to the nearest hundredth:  $\log_5 22$

25) On the coordinate plane below, graph the following.  $f(x) = \log_2 x$  and  $g(x) = 2^x$ . What do you notice about both graphs?

